

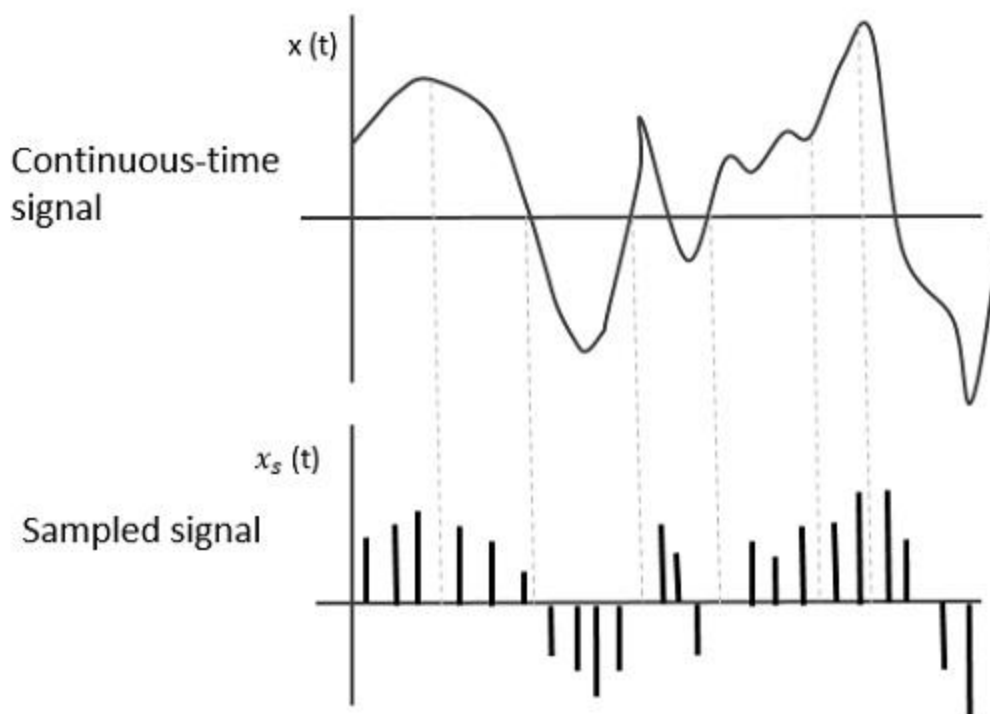
## The Pulse modulation

SO far, we have discussed about continuous-wave modulation. Now it's time for discrete signals. The **Pulse modulation** techniques, deals with discrete signals. Let us see how to convert a continuous signal into a discrete one. The process called Sampling helps us with this.

### Sampling

The process of converting continuous time signals into equivalent discrete time signals, can be termed as **Sampling**. A certain instant of data is continually sampled in the sampling process.

The following figure indicates a continuous-time signal  $x(t)$  and a sampled signal  $x_s(t)$ . When  $x(t)$  is multiplied by a periodic impulse train, the sampled signal  $x_s(t)$  is obtained.



A **sampling signal** is a periodic train of pulses, having **unit amplitude**, sampled at equal intervals of time  $T_s$ , which is called as the **Sampling time**. This data is transmitted at the time instants  $T_s$  and the carrier signal is transmitted at the remaining time.

### **Sampling Rate**

To discretize the signals, the gap between the samples should be fixed. That gap can be termed as the **sampling period**  $T_s$ .

$$\text{Sampling Frequency} = \frac{1}{T_s} = f_s$$

Where,

$T_s$  = the sampling time

$f_s$  = the sampling frequency or sampling rate

### **Sampling Theorem**

While considering the sampling rate, an important point regarding how much the rate has to be, should be considered. The **rate of sampling** should be such that the data in the message signal should neither be lost nor it should get over-lapped.

The **sampling theorem** states that, “a signal can be exactly reproduced if it is sampled at the rate  $f_s$  which is greater than or equal to twice the maximum frequency  $W$ .”

To put it in simpler words, for the effective reproduction of the original signal, the sampling rate should be twice the highest frequency.

Which means,

$$f_s \geq 2W$$

Where,

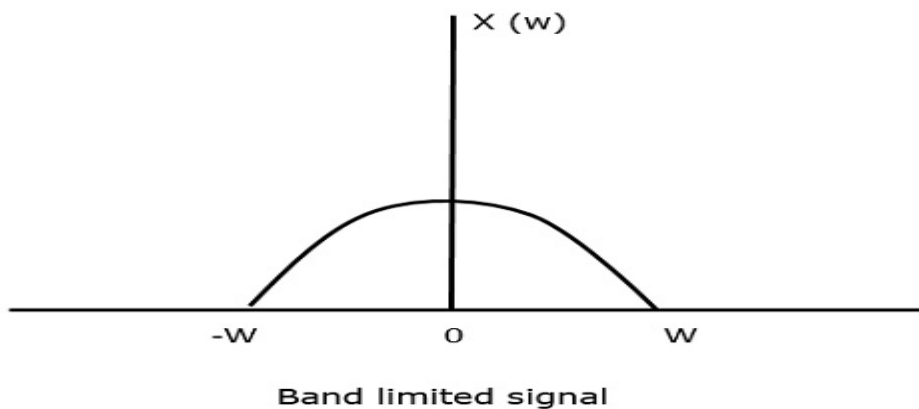
$f_s$  = the sampling frequency

$W$  is the highest frequency

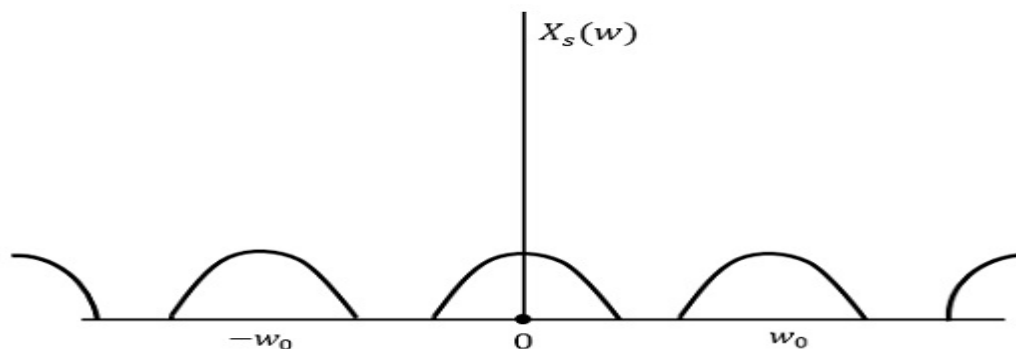
This rate of sampling is called as **Nyquist rate**.

The sampling theorem, which is also called as **Nyquist theorem**, delivers the theory of sufficient sample rate in terms of bandwidth for the class of functions that are bandlimited.

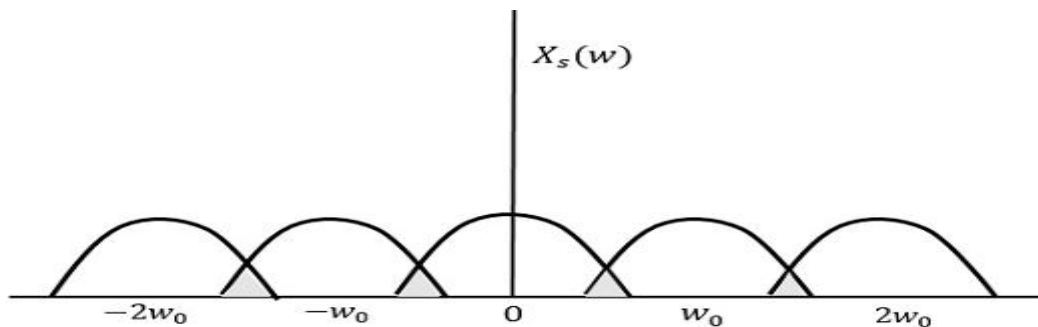
For the continuous-time signal  $x(t)$ , the band-limited signal in frequency domain, can be represented as shown in the following figure.



If the signal is sampled above the Nyquist rate, the original signal can be recovered. The following figure explains a signal, if sampled at a higher rate than  $2W$  in the frequency domain.



If the same signal is sampled at a rate less than  $2w$ , then the sampled signal would look like the following figure.



We can observe from the above pattern that the over-lapping of information is done, which leads to mixing up and loss of information. This unwanted phenomenon of over-lapping is called as **Aliasing**.

Aliasing can be referred to as “the phenomenon of a high-frequency component in the spectrum of a signal, taking on the identity of a lower-frequency component in the spectrum of its sampled version.”

Hence, the sampling of the signal is chosen to be at the Nyquist rate, as was stated in the sampling theorem. If the sampling rate is equal to twice the highest frequency ( $2W$ ).

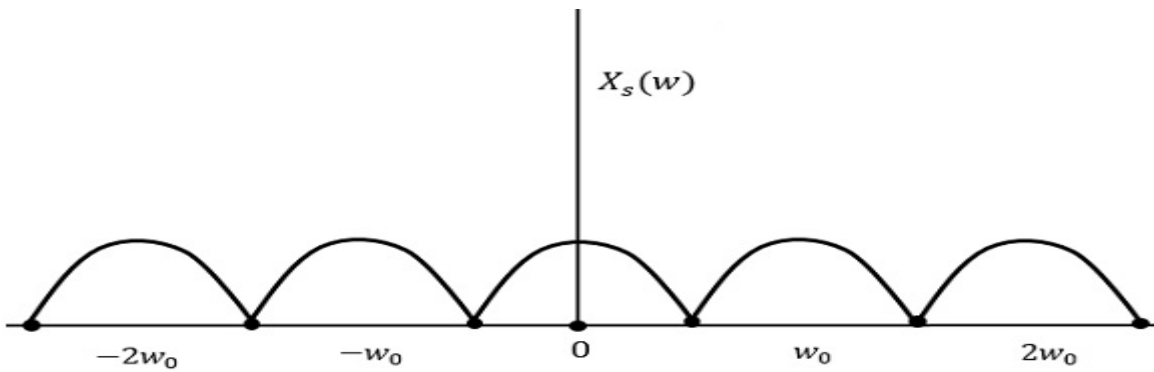
That means,

$$f_s = 2W$$

Where,

$f_s$  = the sampling frequency

$W$  is the highest frequency



The result will be as shown in the above figure. The information is replaced without any loss. Hence, this is a good sampling rate.